Revisiting Time-Memory Trade-offs in Secure Cryptographic Implementations on Resource Constrained Devices

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Motivation



Information Security & Cryptography

Information Security: study of techniques to prevent unauthorised access or use of information.

Basic goals:

- Confidentiality
- Authentication
- Data integrity
- Non-repudiation



Cryptography: provides mathematical foundations and techniques to realise the above goals.



Cryptography

Cryptography has been used since the Roman times, and also in the World Wars.



Figure: Enigma Cipher Machine





Cryptanalysis & Core Problems

Cryptanalysis: study of techniques to defeat the goals of cryptographic primitives and protocols.

Core problems in traditional cryptography (upto 1980s)

- Key establishment
- Secure communication
 - Confidentiality
 - Integrity



Cryptanalysis & Core Problems



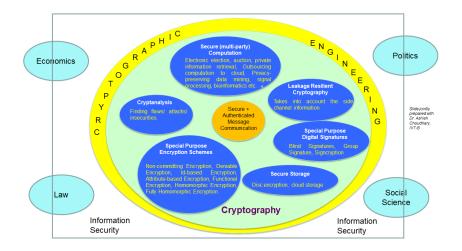
Figure: Evesdropping Adversary

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Slide 5

Domain of Cryptology in Information Security





Traditionally, cryptosystems were viewed as black-boxes.

Change of view in the crypto research community since mid-90s due to Kocher et al.



Figure: Adversary inspecting an execution



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Pre-history of implementation-based attacks

- WWI: Eavesdropping field telephones.
- WWII: Bell Labs electromagnetic side-channel attack.
- MI5/GCHQ acoustic side-channel attacks.
- ► TEMPEST: US government classified program.



Examples:

- Timing attacks
- Power analysis attacks
 - Simple power analysis
 - Differential power analysis
 - Template attacks
- Electro-magnetic attacks
- Cache attacks
- Others: acoustics, thermal, photonic emmision attacks

Different operations + data \implies Different physical "leakage".



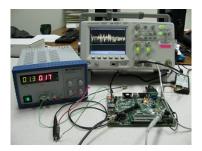


Figure: PAA experiment setup



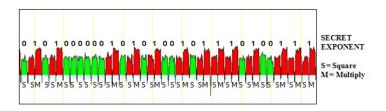


Figure: SPA attack on an RSA implementation



Practical threat for embedded device implementations.

- Microcontrollers and smart cards vulnerable to power analysis attacks.
- Other IoT devices are vulnerable too.

Even advanced architectures are prone to cache, timing, and power attacks.

Possible to mount side-channel attacks *remotely* by injecting malware.

"Attacks only get better" – K. G. Patterson.

SCA & countermeasures - active research area since two decades.



Countermeasures against SCA

Goal: minimise the effect of side-channel leakage.

In this talk, we focus only on countermeasures against power analysis attacks.

Countermeasures against PAA can be broadly categorised as:

- Make the leakage of the device independent of intermediate variables.
 - E.g: *Hiding countermeasure*
- Make intermediate variables independent of secret variables.
 - E.g.: Masking countermeasure



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Masking Countermeasure

Masking: a popular countermeasure against *DPA* attacks.

Well-suited to protect block cipher s/w and h/w implementations.

Method: each sensitive variable $x \in \mathbb{F}_{2^n}$ is secret shared.

 $X = x_0 \oplus x_1 \oplus \ldots \oplus x_v$

 Security: (any subset of) intermediate variables are independent of x.

Security offered has been relatively well analysed

- probing [ISW03] & noisy leakage model [CJJR99, RP13, DDF14].
- Loosely speaking, SCA complexity is exponential w.r.t. v.

[ISW03] Y. Ishai, A. Sahai, D. Wagner. Private circuits: Securing hardware against probing attacks. CRYPTO'03. [CJ/RR99] S. Chari, C.S. Jutla, J.R. Rao, P. Rohatgi. Towards sound approaches to counteract PAA. CRYPTO'99. [RP10] M. Rivain, E. Prouff. Provably secure higher-order masking of AES. CHES'10. [DDF14] A. Duc, S. Dziembowski, S. Faust. Unifying Leakage Models: From Probing Attacks to Noisy Leakage. EUROCRYPT'14.



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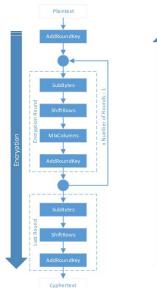


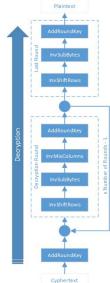
Masking of Block Ciphers

Block cipher: a symmetric-key cryptographic primitive used in many cryptographic constructions

► *E.g.*: DES, AES, PRESENT, etc.







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Slide 14



Masking of Block Ciphers

Linear/Affine functions are straightforward to compute in presence of shares.

- $f(x) = f(x_0) \oplus f(x_1) \oplus \ldots \oplus f(x_v)$
- Time and randomness complexity are both linear in the number of shares.

Main challenge is to securely compute *non-linear* functions.

- Various masking schemes differ mainly in how these functions are evaluated.
- For block ciphers, this reduces to securing their S-boxes.



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Table-based S-box Masking

Originally proposed in [CJJR99].

Input:

- ▶ (*n*, *m*)-S-box
- Two input shares x_1 , x_2 , s.t.

 $x = x_1 \oplus x_2$

Output:

Two output shares y_1 , y_2 , s.t.

 $S(x)=y_1\oplus y_2$



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Method:

Create a temporary table *T* in RAM s.t.

$$T(a) = S(x_1 \oplus a) \oplus y_1 \qquad \forall \ a \in \{0,1\}^n$$

• Compute:
$$y_2 = T(x_2)$$

Output shares: y₁, y₂

Correctness: $S(x) = y_1 \oplus y_2$

1-O Security: first-order secure in the probing model.

Every intermediate variable (incl. i/o) independent of x.



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For an (n, m)-S-box:

- ▶ Pre-processing (offline) run time: $O((n+m) \cdot 2^n)$
- Look-up (online) time: O(n + m)
- **RAM memory**: $O(m \cdot 2^n)$ bits
- Randomess: None

AES: time overhead factor: 2 to 4, RAM memory = 256 bytes.

RAM Memory can be *expensive* for highly resource-constrained environments.

Alternate approaches exist ([*PR07*]): O(1) RAM but time overhead factor ≥ 30 .

[PR07] E. Prouff, M. Rivain. A generic method for secure Sbox implementation. WISA'07.



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Look-up Table Compression

A look-up table compression scheme was proposed in [RRST02].

RAM Memory reduced by a factor ℓ .

- **Compression level**: ℓ (1 $\leq \ell \leq m$)
- Size of Table $T \approx \frac{(m \cdot 2^n)}{\ell}$ bits

Time-memory trade offs by varying ℓ

- ▶ bigger $\ell \Rightarrow$ lesser RAM
- bigger $\ell \Rightarrow$ greater online time

[*RRST02*] J.R. Rao, P. Rohatgi, H. Scherzer, S. Tinguely. *Partitioning attacks: Or how to rapidly clone some GSM cards.* IEEE S&P'02.



Improved First-Order Look-up Table Compression

An *improved* look-up table compression scheme was by Vadnala [*Vad17*].

Variant of [RRST02].

RAM Memory reduced by a factor $\approx 2^{\ell}$ (instead of ℓ).

- Compression level: ℓ (1 $\leq \ell \leq$ n)
- Size of Table $T \approx m \cdot 2^{n-\ell} + (n-\ell) \cdot 2^{\ell}$ bits

Time-memory trade offs by varying ℓ

[Vad17] P.K. Vadnala. Time-memory trade-offs for side-channel resistant implementations of block ciphers. CT-RSA'17.



Idea: "pack" 2^{ℓ} table entries of the original T.



Step 1: create Table $T_1 : \{0,1\}^{n-\ell} \to \{0,1\}^m$ s.t.

$$T_1(a^{(1)}) = \left(\bigoplus_{i \in \{0,1\}^{\ell}} S((a^{(1)} \oplus r_i) || i) \right) \oplus y_1, \quad \forall \ a^{(1)} \in \{0,1\}^{n-\ell}$$

▶ $r_i \in \{0,1\}^{n-\ell}$ uniform random and independent

► y₁: an output share

Randomess complexity: 2^{ℓ} (*n* – ℓ -bit) words.

Recall: original table-based method needs no additional randomness.



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$$a = \underbrace{a^{(1)}}_{n-\ell} || \underbrace{a^{(2)}}_{\ell}$$

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Let the (secret) input be x

$$x = \underbrace{x^{(1)}}_{n-\ell} || \underbrace{x^{(2)}}_{\ell}$$

Step 2: "create" Table $U : \{0,1\}^{\ell} \rightarrow \{0,1\}^{m}$ in RAM s.t.

$$U(i) = S(x^{(1)} || i) \oplus y_1, \quad \forall i \in \{0, 1\}^{\ell}$$

by "securely" accessing tables T_1 and S.

NOTE: *U* cannot be directly computed from *S* and *x*.

Step 3: "securely" compute the second output share

$$y_2 = U(x^{(2)}) = S(x) \oplus y_1$$

NOTE: Actually need Table T_2 = Table U shifted by shares of $x^{(2)}$



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Our Contribution - Part 1



Improving Randomness Complexity

We improved the **randomness complexity** of the first-order secure table compression masking scheme from [*Vad17*].

Still retaining first-order security (in the probing model).

New randomness complexity is $\approx \ell$ ($n - \ell$ -bit) words, *instead* of $\approx 2^{\ell}$ ($n - \ell$ -bit) words.

We prove that the achieved complexity is **optimal**.

RAM memory remains unchanged.

Running time "essentially" remains unchanged on big-architectures.

May possibly improve for highly-resource constrained environments.



Improving Randomness Complexity: Our Method

Recall: first step in [*Vad17*] needs to generate $r_i \stackrel{\$}{\leftarrow} \{0, 1\}^{n-\ell}$

$$T_1(a^{(1)}) = \left(\bigoplus_{i \in \{0,1\}^{\ell}} S((a^{(1)} \oplus r_i) || i) \right) \oplus y_1, \quad \forall \ a^{(1)} \in \{0,1\}^{n-\ell}$$

Our Idea

- Sufficient for r_i to be **pair-wise independent** (and unif. random).
- Sample $\ell + 1$ no. of $\gamma_j \stackrel{\$}{\leftarrow} \{0, 1\}^{n-\ell}$.
- Compute r_i as **subset xor sum** of γ_j .
- Rest of the method essentially remains the same

One extra γ is needed as otherwise $r_0 = 0$.

Security proof: enumerate all intermediate variables and show independence.



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Randomness Complexity: Proof of Optimality

Algebraic lower bound: At least ℓ values of γ_i are needed.

Computation model: only \mathbb{F}_2 -linear operations are performed.

(Nearly) all the known table-based masking schemes use **only xor** for arithmetic operations.

Proof idea: assume only $\mathbf{t} < \ell$ many γ_j were used.

 $r_i = c_i \bigoplus_{1 \le j \le t} b_j \cdot \gamma_j$, where $b_j \in \mathbb{F}_2$, $c_i \in \{0, 1\}^{n-l}$ e exist r_p , r_q $(p \ne q)$ s.t.

$$r_p \oplus r_q = c_p \oplus c_q$$

Then an intermediate variable depends on bits of x

$$ind_2 = x^{(1)} \oplus c_p \oplus c_q$$



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There exist $r_p, r_q \ (p \ne q)$ s.t.

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Our Contribution - Part 2



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Attack on the 2-O Table Compression Scheme [Vad17]

[Vad17] also proposed a **second-order** table compression scheme

- Generalisation of the first-order method.
- Claimed to be second-order secure in the probing leakage model.

We **contradict** the second-order security

Attack: there exist several pairs of intermediate variables that jointly depend on the secret input.



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Three steps *similar* to the first-order scheme.

Step 1: Create Table $T_1 : \{0, 1\}^{n-\ell} \rightarrow \{0, 1\}^m$



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Three steps *similar* to the first-order scheme.

Step 1: Create Table $T_1: \{0,1\}^{n-\ell} \rightarrow \{0,1\}^m$

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$$T_{2}(b^{(2)}) := T_{1}(v^{(1)} \oplus r_{(x_{3}^{(2)} \oplus a^{(2)})}) \oplus \bigoplus_{j \in \{0,1\}^{\ell}, j \neq a^{(2)}} S_{(x_{3}^{(2)} \oplus j)}(x^{(1)} \oplus r_{(x_{3}^{(2)} \oplus a^{(2)})} \oplus r_{(x_{3}^{(2)} \oplus j)})$$



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Step 2: Create Table $T_2 : \{0,1\}^\ell \to \{0,1\}^m$

Step 3: Access Table T_2 to compute the third output share.

$$y_3 = T_2(v^{(2)})$$



Our Attack on 2-O Scheme of [Vad17]

We show that any pair of entries in Table T_2 jointly leak up to $n - \ell$ bits of x.

Lemma

Let $\beta_1, \beta_2 \in \{0, 1\}^I$. Then $T_2(\beta_1) \oplus T_2(\beta_2) = S(\mathbf{x}^{(1)} || (\beta_1 \oplus x^{(2)} \oplus v^{(2)}))$ $\oplus S(\mathbf{x}^{(1)} || (\beta_2 \oplus x^{(2)} \oplus v^{(2)}))$



Our Attack on 2-O Scheme of [Vad17]

We show that any pair of entries in Table T_2 jointly leak up to $n - \ell$ bits of x.

Implies when $\ell = 1$ all but one bit of x may leak

Attack does not apply for

- ℓ = 0
- ► *l* = *n*
- ▶ if output of *S* only depends on least significant *ℓ* bits of input



Conclusion

We improved the randomness complexity of 1-O table compression scheme in [*Vad17*].

Time & memory complexity essentially remains unchanged.

The new randomness complexity is optimal in an algebraic sense.

Attack on the 2-O table compression scheme in [Vad17].

Open problem: to construct second + higher-order table compression schemes.



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Thank You! & Questions?



Reference

Srinivas Vivek, Revisiting a Masked Lookup-Table Compression Scheme, INDOCRYPT 2017.



Slide 33

Sources of images:

- Internet of Things (on Slide 3): www.bestvpn.com
- Enigma cipher (on S. 4): www.extravaganzi.com
- Evesdropping (on S. 5): www.harekrsna.de, www.dollsofindia.com, www.reddit.com, www.globe-views.com
- SCA attack depiction (on S. 7): www.tau.ac.il
- SCA experiment setup (on S. 9): www.cesca.centers.vt.edu
- SPA attack on RSA (on S. 9): www.eetimes.com
- AES encryption/decryption (on S. 13): www.arduinolab.net

